Basic Statistics

Eric Thrane

May 30, 2012

1 Probability distributions and test statistics

See Table 1. Greek letters are known a priori, roman letters are measured.

2 Useful identities

For mean-zero Gaussian random variables, we can expand a four-point correlation into a sum of products of two-point correlations:

$$\langle abcd \rangle = \langle ab \rangle \langle cd \rangle + \text{permutations.}$$
 (1)

hypothesis	condition	test statistic	test distribution
$\mu = \mu_0$	σ^2 known	$\frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$	N(0,1)
$\mu = \mu_0$	σ^2 unknown	$\frac{\bar{x} - \mu_0}{s / \sqrt{n}}$	t(n-1)
$\sigma^2 = \sigma_0^2$	μ known	$\frac{(n-1)s^2}{\sigma_0^2}$	$\chi^2(n)$
$\sigma^2 = \sigma_0^2$	μ unknown	$\frac{(n-1)s^2}{\sigma_0^2}$	$\chi^2(n-1)$
$\mu_1 = \mu_2$	σ_1^2 and σ_2^2 known	$\frac{\bar{x} - \bar{y}}{\sqrt{\sigma_1^2/n + \sigma_2^2/m}}$	N(0,1)
$\mu_1 = \mu_2$	$\sigma_1^2 = \sigma_2^2$ unknown	$\frac{\bar{x} - \bar{y}}{s\sqrt{1/n + 1/m}}$	t(n+m-2)
$\mu_1 = \mu_2$	$\sigma_1^2 \neq \sigma_2^2$ unknown	$\frac{\bar{x} - \bar{y}}{\sqrt{s_1^2/n + s_2^2/m}}$	$\approx N(0,1)$
$\sigma_1^2 = \sigma_2^2$	μ_1 and μ_2 known	s_1^2/s_2^2	F(n,m)
$\sigma_1^2 = \sigma_2^2$	μ_1 and μ_2 unknown	s_1^2/s_2^2	F(n-1,m-1)

Table 1: Choosing the right distribution.